<<计数组合学导引>>

图书基本信息

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前言

What could be a more basic mathematical activity than counting thenumber of elements of a finite set? The misleading simplicity that definesthe subject of enumerative combinatorics iS in fact one of its principalcharms. Who would suspect the wealth of ingenuity and of . sophisticated techniques that can be brought to bear on a such an apparently superficial endeavor?

Mikl6s B6na has done a masterful iob of bringing an overview of a11 of enumerative combinatorics within reach of undergraduates . Thetwo fundamental themes of bijective proofs and generating functions , to-gether with their intimate connections , recur constantly . A wide selection of topics , including several never appearing before in a textbook , are in-cluded that give an idea of the vast range of enumerative combinatorics . In particular , for those with sufficient background in undergraduate lin-ear algebra and abstract algebra there are many tantalizing hints of the fruitful connection between enumerative combinatorics and algebra thaltplays a central role in the subject of algebraic combinatorics . In a fore-word to another book by Mikl6s B6na 1 wrote , " This book can be utilized at a variety of levels , from random samplings of the treasures therein to acomprehensive attempt to master all the material and solve all the exer-cises . In whatever direction the reader 'S tastes lead , a thorough enjoymentand appreciation of a beautiful area of combinatorics iS certain to ensue . " Exactly the same sentiment applies to the present book , as the reader willsoon discover .

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内容概要

The book can be used in at least three ways. One can teach a onesemester course from it , choosing the most general topics. One can alson use the book for a two-semester course , teaching most of the text and exploring the supplementary material that is given in form of exercises. If one has already taught a one-semester course using a general Combi-natorics textbook and wants to follow up with a second semester that focuses on enumeration , one may use the last six chapters of this book. The book is also useful for teaching an introductory course for graduate students who do not have solid background in Combinatorics. There are several topics here that are discussed in detail in an under-graduate textbook for a first time , such as acyclic and parking functions , unimodality , log-concavity , the real zeros property , and magic squares. Therefore , we hope the book will provide a useful reference material for students interested in these topics.

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作者简介

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章节摘录

插图: Assume we want to send a message from our cell phone using justthe two-letter binary alphabet consisting of the letters 0 and 1. Say themessage that we want to send is a YES or NO message. We could agreewith the recipient that I means yes, and 0 means no. This is simple enoughif we are both sure that we will not make any mistakes in typing. However, if mistakes are possible, then this way of encoding messageswill not be efficient. Indeed, one single mistake could totally turn themeaning of the message into its opposite. One way to make sure thatour message is not misunderstood is to send it over and over again, inconsecutive bits. Say that we will send our message three times. If themessage is YES, then we will send the digits 111, and if the messageis NO, then we will send the digits 000. These two codewords are notat all similar to each other. Therefore, if we are sure that at most onetyping mistake will be made, we can rest assured that our message willbe understood properly. Indeed, if we want to send the codeword 111 (resp. 000), and at most one mistake will be made, then the receivedword will contain at least two ls (resp. at least two 0s). So as long as atmost one bit is erroneous in each codeword, all errors can be corrected. This simple example can be generalized in many different directions. First, it could be that there are more than just two possible messagesto send. Second, it could also be that there are more than two digits inour coding alphabet. Third, more than one mistake may be made during typing. Nevertheless, the main idea of our simple example is crucial. Thisidea is that if the codewords are sufficiently dissimilar from each other, then we can teU them apart even if a few mistakes are made. It is time that we made the notions of "sufficiently dissimilar" and "few mistakes" more precise.

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媒体关注与评论

Mikl6s B6na has done a masterful job of bringing an overview of all of enumerativecombinatorics within reach of undergraduates. The two fundamental themes of bijective proofs and generating functions, together with their intimate connections, recur constantly. A wide selection of topics, including several never appearing beforein a textbook, are included that give an idea of the vast range of enumerativecombinatorics. In particular, for those with sufficient background in undergraduatelinear algebra and abstract algebra there are many tantalizing hints of the fruitfulconnection between enumerative combinatorics and algebra that plays a central rolein the subject of algebraic combinatorics.

——Richard Stanley Cambridge, Massachusetts

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